## Textbook Information Math 207 GH – Calculus and Analytic Geometry I Fall 2017

## Lecture Notes, Worksheets

Most topics covered in the class will be presented via handouts. These will be available at the <u>class's web site</u>, as pdf files. All students must monitor the class's web site for handouts and announcements.

## Textbook

The class's textbook policy is as follows. **Students must have a textbook but it does NOT have to be the official textbook designated for this course.** This policy is intended to lower textbook costs. Usually students can purchase a textbook for the course under \$40. Students are welcome to use any previous edition at a much lower cost. Students also may rent or purchase e-versions of a calculus book.

The Mathematics Department selected Calculus 7E by Hughes-Hallett. Due to price considerations, the use of this book will not be mandatory in this class.

As this is an excellent text, students are encouraged to buy a previous edition of this textbook. Students also may use other calculus books. However, it is essential that students use a text that is labeled **early transcendentals**. (That is what the E stands for in 7E.) Other, excellent texts include any early transcendental version (any edition) of calculus textbooks written by:

Soo T. Tan George B Thomas Ron Larson Jerrold E. Marsden James Stewart William Briggs

Open source textbooks are also available. Open source means free pdf download, in this case, here: <u>https://openstax.org/subjects/math</u>. Students are encouraged to download and use the open source calculus textbooks.

## **Online Homework**

Homework will be assigned on MyOpenMath, an open source online platform. The use of MyOpenMath is completely free, and students can register at <u>https://www.myopenmath.com</u>. The use of MyOpenMath will be mandatory in the class.

# **Contents of Textbook**

#### 1. Foundations for Calculus: Functions and Limits

- 1.1 Functions and Change
- 1.2 Exponential Functions
- 1.3 New Functions from Old
- 1.4 Logarithmic Functions
- 1.5 Trigonometric Functions
- 1.6 Powers, Polynomials, and Rational Functions
- 1.7 Introduction to Limits and Continuity
- 1.8 Extending the Idea of a Limit
- 1.9 Further Limit Calculations Using Algebra

#### 2. Key Concept: The Derivative

- 2.1 How Do We Measure Speed?
- 2.2 The Derivative at a Point
- 2.3 The Derivative Function
- 2.4 Interpretations of the Derivative
- 2.5 The Second Derivative
- 2.6 Differentiability

#### 3. Short-Cuts to Differentiation

- 3.1 Powers and Polynomials
- 3.2 The Exponential Function
- 3.3 The Product and Quotient Rules
- 3.4 The Chain Rule
- 3.5 The Trigonometric Functions
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- 3.7 Implicit Functions
- 3.8 Hyperbolic Functions
- 3.9 Linear Approximation and the Derivative
- 3.10 Theorems About Differentiable Functions

#### 4. Using the Derivative

- 4.1 Using First and Second Derivatives
- 4.2 Optimization
- 4.3 Optimization and Modeling
- 4.4 Families of Functions and Modeling
- 4.5 Applications to Marginality
- 4.6 Rates and Related Rates
- 4.7 L'Hopital's Rule, Growth, and Dominance
- 4.8 Parametric Equations

#### 5. Key Concept: The Definite Integral

- 5.1 How Do We Measure Distance Traveled?
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- 5.3 The Fundamental Theorem and Interpretations
- 5.4 Theorems About Definite Integrals

#### 6. Constructing Antiderivatives

- 6.1 Antiderivatives Graphically and Numerically
- 6.2 Constructing Antiderivatives Analytically
- 6.3 Differential Equations and Motion
- 6.4 Second Fundamental Theorem of Calculus

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- 7.1 Integration by Substitution
- 7.2 Integration by Parts
- 7.3 Tables of Integrals
- 7.4 Algebraic Methods for Definite Integrals
- 7.5 Numberical Methods for Definite Integrals
- 7.6 Improper Integrals
- 7.7 Comparison of Improper Integrals

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#### 8. Using the Definitive Integral

- 8.1 Areas and Volumes
- 8.2 Applications to Geometry
- 8.3 Area and Arc Length in Polar Coordinates
- 8.4 Density and Center of Mass
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- 8.7 Distribution Functions
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- 9.4 Tests for Convergence
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- 10.5 Fourier Series

#### 11. Differential Equations

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- 11.2 Slope Fields
- 11.3 Euler's Method
- 11.4 Separation of Variables
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- 11.7 The Logistic Model
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14. Differentiating Functions of Several Variables

14.4 Gradients and Directional Derivatives in the Plane

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14.5 Gradients and Directional Derivatives in Space

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20.2 Stokes' Theorem

20.3 The Three Fundamental Theorems

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