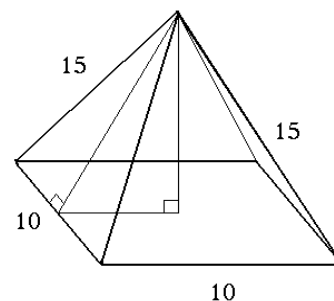


- Suppose that $U = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$, $A = \{1, 2, 3, 4, 5\}$, and $B = \{1, 4, 8, 9\}$, and $C = \{2, 3, 8, 10\}$. Find each of the following.
 - $A \cap B$
 - $A \cup B$
 - $A \cup (B \cap C)$
 - $(A \cup B) \cap C$
 - $(A \cap B) \cup C$
 - $A \cap \overline{B}$
 - $\overline{A \cap C}$
 - $\overline{A \cap B}$
 - $\overline{A \cup B}$
 - $\overline{A \cup C}$
 - $\overline{(A \cap C) \cup B}$
- Compute each of the following sets.
 - $(1, 5) \cup [2, 8]$
 - $(1, 5) \cap [2, 8]$
 - $(-\infty, 5) \cup (-2, \infty)$
 - $(-\infty, 5) \cap (-2, \infty)$
 - $(3, 4) \cup [1, 7]$
 - $(3, 4) \cap [1, 7]$
 - $(-\infty, -3) \cup (-1, 12)$
 - $(-\infty, -3) \cap (-1, 12)$
- Label each of the following statements as true or false.
 - If a natural number n is divisible by 6, then its square is divisible by 18.
 - For all sets A , $A \cap \emptyset = \emptyset$.
 - For all sets A and B , if $A \cup B = A$, then A is a subset of B .
 - For all sets A and B , if $A \cup B = A$, then B is a subset of A .
 - Suppose that x and y are positive integers. If the product xy is divisible by 3, then x is divisible by 3 or y is divisible by 3.
 - Suppose that x and y are positive integers. If the product xy is divisible by 6, then x is divisible by 6 or y is divisible by 6.
 - There is no right triangle with all three sides odd integers.
- Let $M = 2^{100}$. Write each of the following expressions in terms of M .
 - $2^{100} - 2^{101} + 2^{102} - 2^{103}$
 - $2^{103} - 5 \cdot 2^{102}$
 - 4^{100}
 - 2^{200}
 - 2^{500}
 - 2^{99}
- Simplify each of the following expressions.
 - $(\sqrt[3]{x})^{12}$
 - $\sqrt{x^{100}}$
 - $\left((-x)^3(-x^4)\right)^5$
 - $\left((-x)^3(-x^2)^{-4}\right)^{-1}$
 - $\frac{12x - 8}{-4}$
 - $\sqrt{125} - 3\sqrt{80} + \sqrt{45}$
 - $(\sqrt{7} - 2)^2$
 - $(\sqrt{3} - 1)^3(\sqrt{3} + 1)^3$
 - $\frac{\sqrt{40}}{6}$
 - $\frac{2^{-2} 3^{-1}}{2^0 3^{-2}}$
 - $\left(\frac{-2a^0ba^{-5}}{3a^{-2}b^2a^{-3}}\right)^{-3}$
 - $\frac{-2a^7b^0(2a^5b^{-3}a^{-1})^{-1}}{b^5(4a^{-3}b^2)^{-3}(-a)^{-4}}$
- Expand each of the following.
 - $(3x - 1)^2$
 - $(3x - 1)^3$
 - $(3x^2 - 2)^2$
 - $(x - y)(x^2 + xy + y^2)$
- Rationalize the denominator in each of the following expressions.
 - $\frac{3}{\sqrt{5}}$
 - $\frac{1}{\sqrt{10} - 3}$
 - $\frac{2}{\sqrt{7} + 1}$
 - $\frac{3 + \sqrt{3}}{3 - \sqrt{3}}$
 - $\frac{2\sqrt{x}}{\sqrt{x} - 3}$
- Convert each of the following decimals to a fraction of integers.
 - 1.037
 - $0.78\overline{70}$
 - $0.61\overline{8}$
- Compute each of the following sums.
 - $8 + 16 + 24 + \dots + 2016$
 - $20 + 23 + 26 + \dots + 98$
 - $320 + 335 + 350 + \dots + 2120$

10. A conference had 50 attendees, 35 men and 15 women.
- If every attendee shook hands with everyone else, how many hand shakes took place?
 - If women greet *only* women with a hand shake, and men greet *only* men with a hand shake, how many hand shakes took place?
11. Factor each of the following over the real numbers **by completing the square**.
- $3x^2 - 7x - 6$
 - $x^2 - 6x + 4$
 - $3x^2 + 2x - 2$
12. Completely factor each of the following over the real numbers.
- $x^2 - y^2 + 2y - 1$
 - $24x - 9x^2 - 16$
 - $3a^2 - 5a - 2$
 - $30x - 3x^2 - 78$
 - $13x + 2x^2 - 24$
 - $x^2 - 6x + 8$
 - $4b^2 - b - 5$
 - $5a^5 - 80a$
13. Solve each of the following equations over the real numbers. Make sure to check your solution(s).
- $2x^3 = 20x^2 + 1750x$
 - $\frac{2}{3}(x - 7) = \frac{4}{5}(x + 1)$
 - $x^2 = 4x + 1$
 - $\frac{3x + 17}{2} = x - 1 + \frac{x + 19}{2}$
 - $8a + 2a^2 = 42$
 - $3x^2 - x = 5x + 1$
 - $\frac{3}{8}x - \frac{1}{5} = -\frac{7}{40}$
 - $8p^3 = 50p$
 - $\frac{2}{3}x - \frac{1}{6} = \frac{3}{5}x + \frac{1}{3}$
 - $x^2 = 4x - 5$
 - $x(x - 5) + 1 = 3(x - 2)$
 - $7x^2 + (x + 3)(2x - 1) = (3x + 1)^2$
 - $2 - (3 - x)(2x + 5) = (x - 1)(2x - 1)$
14. Find the smallest value of the given expressions.
- $x^2 - 20x + 38$
 - $x^4 + 2x^2 - 2$
 - $x^4 - 2x^2 - 2$
15. Find the midpoint of the line segment PQ where $P(-8, 1)$ and $Q(2, 15)$.
16. a) Graph the line $3x - 4y = -5$. Make sure to find two lattice points.
 b) Graph the straight lines $3x + 5y = 5$ and $y = -x - 1$ in the same coordinate system. Use your graph to find the coordinates of the point where the lines intersect.
17. Graph the parabola $y = x^2 - 6x + 5$. Clearly state the coordinates of five points on the parabola, including vertex and intercepts.
18. Solve each of the following inequalities. Present your answer in interval notation.
- $\frac{2x - 1}{3} - \frac{3x + 1}{4} \leq x - 6$
 - $\frac{2}{3}x - \frac{5}{6} \geq -\frac{1}{3}$
 - $(x + 6)^2 < (x + 4)^2$
 - $2(x - 3) - x - 16 > 3x + 2 - 4(1 - 2x)$
19. Find the distance between the points $A(-3, -5)$ and $B(3, 3)$.
20. a) Find the exact value of the area of a triangle with sides 8 m, 6 m, and 6 m long.
 b) Find the exact value of the area of a regular triangle with sides 5 meters long.
21. An arch is in the shape of a semicircle. At a point along the base 1 foot from an end of the arch, the height of the arch is 5 feet. Find the maximum height of the arch. Present exact value of the answer.
22. Compute the perimeter and area of the parallelogram determined by the points $A(1, 3)$, $B(5, 6)$, $C(5, 15)$, and $D(1, 12)$.

23. The picture shows a straight pyramid with a square base. The sides of the base are 10 in long. The other sides are 15 in long.
- Find the exact value of the height of a triangular face. This is called the slant height.
 - Use part a) to find the height of the pyramid.
24. Find the sides in a rectangle if we know that one side is 12 cm and the diagonal of the rectangle is 2 cm longer than the other side.
25. Solve each of the following word problems.



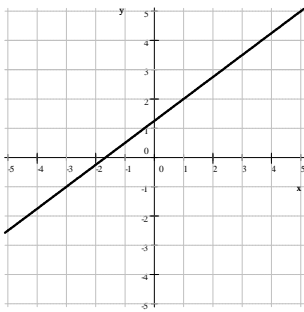
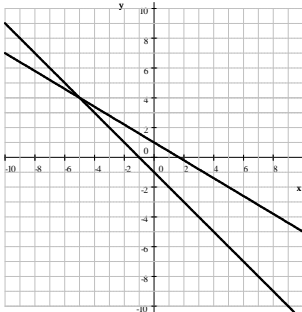
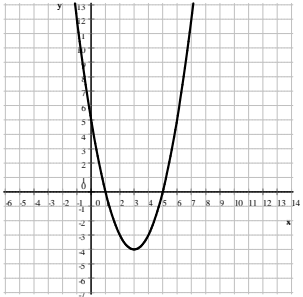
- One side of a rectangle is 4 ft shorter than three times the other side. Find the sides if the perimeter is 64 ft.
- One side of a rectangle is 4 ft shorter than three times the other side. Find the sides if the area is 84 ft^2 .
- One side of a rectangle is 4 in shorter than 3 times the other side. Find the sides of the rectangle if its area is 319 in^2 .
- A bank teller has some five-dollar bills and ten-dollar bills. The number of five-dollar bills is ten less than twice the number of ten-dollar bills. The total value of the money is \$610. How much of each denomination of bill does he have?
- The first row in a theater has 18 seats in it. The second row has four more seats than the first row. The third row has four more seats than the second row. And so on, each row has four more seats than the row before. If the last row has 114 seats in it, how many seats are there in the entire theater?
- During a volatile day in the markets, our stock has first gained 12% of its value. In a few hours, the stock lost 10% of its value. Express the two changes together as a single change. What percentage of a change is this?
- A total of \$20 000 is to be invested in bonds and stocks. If the amount invested in bonds is to be \$4500 more than the amount invested in stocks, how much money is invested in each category?
- A TV set went on a 12% off sale. If the sale price is \$1848, what was the original price?
- The hypotenuse of right triangle is 50 meters long. The difference between the other two sides is 34 meters. Find the missing sides. Use exact values.
- One real number is 28 less than another. What is the smallest possible value of the product of these numbers?
- Find the sides of the square if we know the following: if we increase each side by 2 cm, the square's area will increase by 48 cm^2 .
- We throw an object upward from the top of a 1904 ft tall building. The vertical position h of the object, (measured in feet) t seconds after we threw it is

$$h = -16t^2 + 160t + 1904$$

How long does it take for the object to hit the ground?

- One number is four less than three times another number. Find these numbers if their sum is 64.
- One number is four less than three times another number. Find these numbers if their product is 160.
- During a volatile day in the markets, our stock has first gained 20% of its value. In a few hours, the stock lost 20% of its value. Express the two changes together as a single change. What percentage of a change is this?
- Eight times a number is nine less than the square of the number. Find this number.
- Sally worked 50 hours last week and made \$660 for the week. For every hour worked over 40 her job pays time and a half. What is Sally's regular hourly pay rate?

Answers

1. a) $\{1, 4\}$ b) $\{1, 2, 3, 4, 5, 8, 9\}$ c) $\{1, 2, 3, 4, 5, 8\}$ d) $\{2, 3, 8\}$ e) $\{1, 2, 3, 4, 8, 10\}$ f) $\{2, 3, 5\}$
g) $\{6, 7, 9\}$ h) $\{2, 3, 5, 6, 7, 8, 9, 10\}$ i) $\{6, 7, 10\}$ j) $\{5, 6, 7, 10\}$
2. a) $(1, 8]$ b) $[2, 5)$ c) $(-\infty, \infty)$ d) $(-2, 5)$ e) $[1, 7]$ f) $(3, 4)$ g) cannot be simplified h) \emptyset
3. a) true b) true c) false d) true e) true f) false g) true
4. a) $-5M$ b) $-12M$ c) M^2 d) M^2 e) M^5 f) $\frac{M}{2}$
5. a) x^4 b) x^{50} c) $-x^{35}$ d) $-x^5$ e) $-3x + 2$ f) $-4\sqrt{5}$ g) $11 - 4\sqrt{7}$ h) 8 i) $\frac{\sqrt{10}}{3}$ j) $\frac{15}{4}$ k) $-\frac{3}{32}$
l) $-\frac{27b^3}{8}$ m) $-\frac{64b^4}{a^2}$ 6. a) $9x^2 - 6x + 1$ b) $27x^3 - 27x^2 + 9x - 1$ c) $9x^4 - 12x^2 + 4$ d) $x^3 - y^3$
7. a) $\frac{3}{\sqrt{5}}$ b) $\sqrt{10} + 3$ c) $\frac{\sqrt{7} - 1}{3}$ d) $2 + \sqrt{3}$ e) $\frac{2x + 6\sqrt{x}}{x - 9}$ 8. a) $\frac{1037}{1000}$ b) $\frac{7792}{9900}$ c) $\frac{557}{900}$
9. a) 255 024 b) 1593 c) 147 620 10. a) 1225 b) 700
11. a) $3\left(x + \frac{2}{3}\right)(x - 3) = (3x + 2)(x - 3)$ b) $(x - 3 + \sqrt{5})(x - 3 - \sqrt{5})$ c) $3\left(x - \frac{-1 + \sqrt{7}}{3}\right)\left(x - \frac{-1 - \sqrt{7}}{3}\right)$
12. a) $(x - y + 1)(x + y - 1)$ b) $2(x + 8)\left(x - \frac{3}{2}\right) = (x + 8)(2x - 3)$ c) $-9\left(x - \frac{4}{3}\right)^2$ d) $(x - 2)(x - 4)$
e) $(a - 2)(3a + 1)$ f) $(4b - 5)(b + 1)$ g) $-3(x^2 - 10x + 26)$ h) $5a(a^2 + 4)(a + 2)(a - 2)$
13. a) $-35, 0, 25$ b) identity, solution set: \mathbb{R}
c) $\frac{1}{15}$ d) -41 e) $-7, 3$ f) $\frac{25}{4}, 0$
g) $-\frac{5}{2}, 0, \frac{5}{2}$ h) no real solution i) $2 \pm \sqrt{5}$
j) $\frac{3 \pm 2\sqrt{3}}{3}$ k) $\frac{15}{2}$ l) 1, 7 m) -4 n) 7
14. a) -62 b) -2 c) -3 15. $M(-3, 8)$
16. a)  b) $(-5, 4)$ 
17. y -intercept: $(0, 5)$
vertex: $(3, -4)$
 x -intercepts:
 $(1, 0)$ and $(5, 0)$
additional points:
 $(2, -3)$,
 $(4, -3)$, $(6, 5)$ 
18. a) $[5, \infty)$ b) $(-\infty, -5)$ c) $\left[\frac{3}{4}, \infty\right)$ d) $(-\infty, -2)$
19. 10 units 20. a) $8\sqrt{5} \text{ m}^2$ b) $\frac{25\sqrt{3}}{4} \text{ m}^2$
21. 13 ft 22. $P = 28$ unit, $A = 36$ unit²
23. a) $\sqrt{200} \text{ in} = 10\sqrt{2} \text{ in}$ b) $\sqrt{175} \text{ in} = 5\sqrt{7} \text{ in}$
24. 12 cm by 35 cm
25. a) 9 ft and 23 ft b) 6 ft and 14 ft c) 11 in by 29 in d) 33 ten-dollar bills and 56 five-dollar bills e) 1650
f) 0.8% increase g) \$7750 in stocks and \$12 250 in bonds h) \$2100 i) 14 m, 48 m, 50 m j) -196 k) 11 cm
l) 17 seconds m) 17 and 47 n) 8 with 20 and $-\frac{20}{3}$ with -24 o) 4% decrease p) $-1, 9$ q) \$12