

To receive full credit, show all steps.

1. Simplify each of the following.

(a) $(3x - 7)^2 =$

(b) $(2a^3 - 5b)(2a^3 + 5b) =$

(c) $\frac{2x - 7}{7 - 2x} =$

(d) $\frac{2x + 6}{18x - 2x^3} =$

(e) $\frac{6xy - 2y - 3x + 1}{9x^2 - 1} =$

(f) $\frac{3a - 12}{3a + 15} \cdot \frac{5a + 20}{a^2 - 16} =$

(g) $\frac{7x - 13}{2x - 5} - \frac{7 - x}{2x - 5} =$

(h) $-3^0 - (-3)^0 =$

(i) $3^{-2} \cdot (3^{-3})^{-2} =$

(j) $(3^{-3} \cdot 3^1)^{-2} =$

(k) $2^5 x^{-2} (-2x^{-2})^{-3} =$

(l) $\frac{(-3ab)^3 ab^{-3}}{-3b^{-3} a^2 (3a^{-1}b)^2} =$

(m) $(a + b)(a^4 - a^3b + a^2b^2 - ab^3 + b^4) =$

2. Factor completely each of the following:

(a) $2bnxy - 4anxy + 12anx^2 - 6bnx^2 =$

(b) $75bm^3 - 150am^3 + 24am^5 - 12bm^5 =$

(c) $240a^5p - 160a^5q - 15apx^4 + 10aqx^4 =$

3. Factor by grouping.

(a) $4b + b^2 - 21 =$

(b) $14p^2 - p - 3 =$

(c) $14m + 5m^2 - 3 =$

4. Solve each of the following equations. Make sure to check your solutions.

(a) $\frac{3x - 1}{5} - \frac{7 - x}{3} = x - 2$

(b) $5(x - 2) - (3 - 4x) = 8(x - 2) - (5 - x)$

- (c) $5p^7 = 20p^6$
- (d) $5p^7 = 20p^5$
- (e) $(-1 - 2x) - (3x + 5)(2x - 1) = 3(1 - 2x)(x - 1) + 7$
- (f) $m^2 + 55 = 16m$

5. Solve each of the following inequalities. Graph the solution set.

- (a) $\frac{2a + 1}{5} - \frac{7 - a}{2} > -a - 9$
- (b) $\frac{5 - y}{3} \geq -8$
- (c) $(3x - 8) - (4x - 5) > x - 3$

6. Solve each of the following formulas.

- (a) $P = 5x - 2y$ for x .
- (b) $P = 5x - 2y$ for y .
- (c) $V = \frac{\pi r^2 h}{3}$ for h .
- (d) $7a - 3b = 42$ for b .

7. Graph the straight lines $2x + y = 5$ and $y = -x + 1$ in the same coordinate system.

- (a) Use your graph to find the coordinates of the point where the lines intersect.
- (b) Use algebraic methods to check your solution for part a).

8. Word Problems.

- (a) The population of a town has decreased by 10%. Now there are 7650 residents. Find the original population.
- (b) The difference between two numbers is 34, their sum is 20. Find these numbers.
- (c) Ann and Betty are roommates. The monthly rent is \$ 980. The amount paid by Ann is \$ 130 less than twice the amount paid by Betty. How much do they each pay for rent?
- (d) The price of a TV is \$ 680. If this price was to be changed to \$ 442, what percent of a change does this represent?
- (e) One side of a rectangle is 5 ft shorter than twice the other side. Find the sides if the perimeter is 32 ft.
- (f) One side of a rectangle is 5 ft shorter than twice the other side. Find the sides if the area is 150 ft².