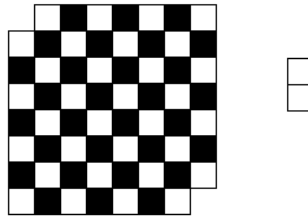
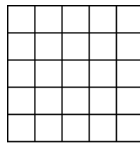


Puzzles

1. Two mathematicians are having a conversation. Mathematician A asks B about his kids. B answers: "I have three children, the product of their ages is 36." A says: "I still don't know how old your children are." Then B tells A the sum of his three kids' ages. A answers: "I still don't know how old they are. Then B adds: "The youngest one has red hair." Now A knows how old the kids are. Do you?
2. Consider a chess board with two corners missing, as indicated on the picture below. We also have 31 pieces of domino, each of them can cover exactly 2 fields on the chess board. Is it possible to cover the chessboard with the domino pieces?

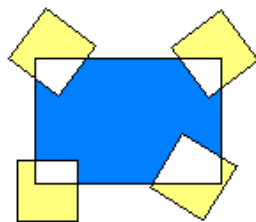


3. A king has his birthday. So he decides to let go some of his prisoners. He actually has 100 prisoners at the moment. They are each in a separate cell, numbered from 1 to 100. Well, he is a high tech king. He can close or open any prison door by a single click on the cell's number on his royal laptop. When he clicks at a locked door, it opens. When he clicks at an open door, it locks. At the beginning, every door is locked. First the king clicks on every number from 1 to 100 (therefore opening every door). Then he clicks on every second number from 1 to 100, (i.e. 2, 4, 6, 8, 10, . . .). Then he clicks on every third number. (i.e. 3, 6, 9, 12, . . .) Now he is opening some doors, locking others. Then he clicks on every fourth number. (i.e. 4, 8, 12, 16,) Then on every fifth, every sixth, every seventh, and so on, until every 100th; finally, he only clicks on the number 100. Then he orders that the prisoners that find their door open may go free. Who gets to go and who has to stay?
4. There is a 5x5 board as the picture below shows. So happens, on each one of the fields there is a ladybug sitting. Suddenly, each decides to move to a neighboring field. (Two fields are neighbors if they have an edge in common.) Is it possible that after each have moved there is again exactly one lady bug sitting on each field?



5. Mr and Mrs Brown are having a party. They invited three other married couples, so there are eight people present. When greeting each other, some people shake hands with some people. Of course, nobody shakes hands with his/her spouse. When Mr Brown asks the other seven people: "How many people did you shake hands with?", he receives seven different answers. How many people did Mrs. Brown shake hands with?

6. The picture below shows a rectangle (the sides' length are 2 and 3 unit long) and four identical squares (all four sides are 1 unit long). Determine which area is greater: the yellow or the blue?



7. We are at a cross road. One road leads into a dangerous swamp, the other road leads into a town. There is a pair of identical twins on the crossing. We know that one twin always tells the truth, the other twin always lies. We are allowed to ask only one question from only one brother. Is there a way to find out which road leads to town?

8. Mindreading. Instructions:

Step 1. Think of a 5-6 digit number, that has at least two different digits in it. My example is 803225.

Step 2. Create a second number by rearranging the digits of the previous number. My example is 320258.

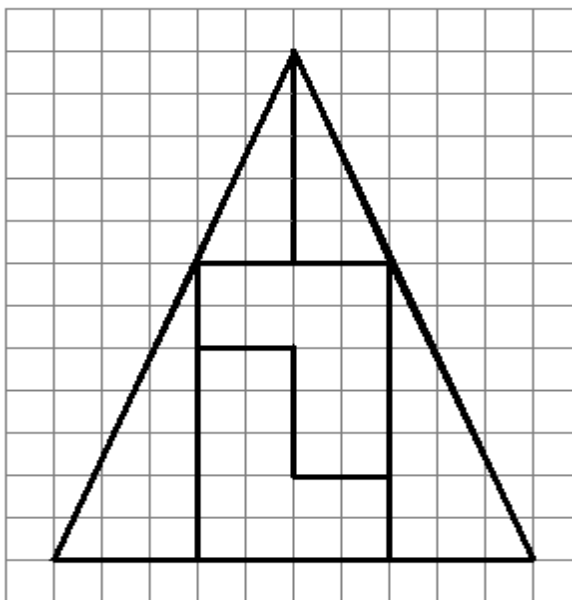
Step 3. Subtract the smaller number from the larger number. My example is $803225 - 320258 = 482967$

Step 4. Cross out any non-zero digit of the difference. My example is 4829~~6~~7.

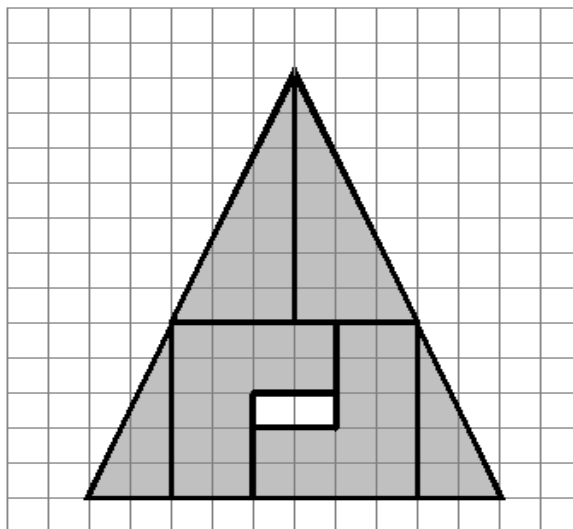
Step 5. Announce the number you obtain by omitting the crossed out digit. My example is 48297.

If you tell the mindreader the last number, s/he can tell what digit you've crossed out. How?

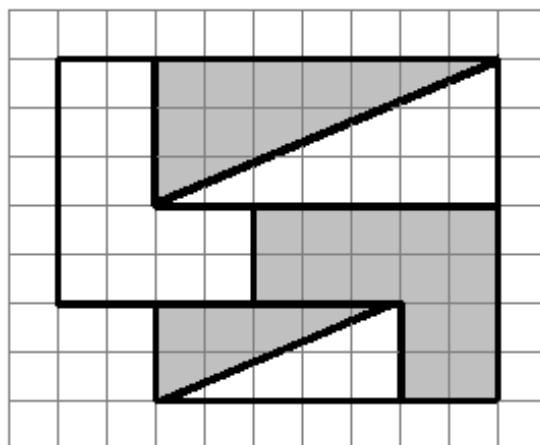
9. (Paul Curry) Imagine that we cut the figure below out of paper. The area of the triangle is $A = \frac{10 \cdot 12}{2} = 60 \text{ unit}^2$.



Suppose we color the other side of the paper, turn the pieces upside down, and rearrange them to obtain the figure shown below.



Now the area appears to be 58 unit^2 since there is a 2 unit^2 area of a whole that the triangle developed. To make matters worse, we now again rearrange the pieces, turning some of them back to the original side.



The area of this figure is $7(9) - 4 = 59 \text{ unit}^2$. Logic tells us that areas of figures do not change if we rearrange them or turn them on their other side. So, what is wrong with these pictures, and how much is really the area of these shapes, 58 unit^2 , 59 unit^2 , or 60 unit^2 ?